

# Busy Beaver's Faulty Machine

Input file:            **standard input**  
Output file:           **standard output**  
Time limit:            1 second  
Memory limit:         256 megabytes

Deep in Busy Beaver's robotics lab sits an experimental Busy Beaver machine. Given a positive integer  $X$  written in base  $B$ , it attempts to produce two positive integers  $Y$  and  $Z$  such that  $X + Y = Z$ , and the base- $B$  representations of  $Y$  and  $Z$  contain exactly the same multiset of digits.

The machine never produces leading zeroes and never outputs numbers with  $2 \cdot 10^5$  or more digits. It has recently stopped functioning, so your task is to determine whether such  $Y$  and  $Z$  exist, and to output them if they do. You are given the digits of  $X$  in base  $B$  without leading zeroes.

## Input

The first line contains a single integer  $T$  ( $1 \leq T \leq 100$ ), the number of test cases.

Each test case consists of two lines. The first line of each test case contains two integers  $N$  and  $B$  ( $1 \leq N \leq 10^5$ ;  $2 \leq B \leq 10^5$ ).

The second line of each test case contains  $N$  integers  $a_1, a_2, \dots, a_N$  ( $0 \leq a_i \leq B - 1$ ;  $a_1 \neq 0$ ), representing the digits of  $X$  in base  $B$ :

$$X = a_1 B^{N-1} + a_2 B^{N-2} + \dots + a_N.$$

The sum of  $N$  over all test cases does not exceed  $2 \cdot 10^5$ .

## Output

For each test case, if no valid solution exists, output a single line containing **NO**.

Otherwise, output **YES** on the first line. On the second line output an integer  $M$  ( $1 \leq M \leq 2 \cdot 10^5$ ), the number of digits in both  $Y$  and  $Z$ .

On the next line output  $M$  digits  $p_1, p_2, \dots, p_M$  ( $0 \leq p_i \leq B - 1$ ;  $p_1 \neq 0$ ), representing

$$Y = p_1 B^{M-1} + p_2 B^{M-2} + \dots + p_M.$$

On the following line output  $M$  digits  $q_1, q_2, \dots, q_M$  ( $0 \leq q_i \leq B - 1$ ;  $q_1 \neq 0$ ), representing

$$Z = q_1 B^{M-1} + q_2 B^{M-2} + \dots + q_M.$$

The digit sequences  $(p_1, \dots, p_M)$  and  $(q_1, \dots, q_M)$  must use exactly the same multiset of digits, and the integers they represent must satisfy  $X + Y = Z$ . You may print **YES** and **NO** in any mixture of uppercase and lowercase letters.

## Example

standard input	standard output
3	YES
2 10	2
3 6	1 5
4 5	5 1
1 4 3 4	YES
5 12	4
4 8 8 3 1	1 4 3 2
	3 4 2 1
	NO

## Note

In the first test case, with  $B = 10$  and  $X = 36$ , a valid solution is  $Y = 15$  and  $Z = 51$ , since  $51 = 36 + 15$  and both numbers use the digits  $\{1, 5\}$ .

In the second test case, with  $B = 5$  and  $X$  given by digits  $(1, 4, 3, 4)_5$ ,

$$X = 1 \cdot 5^3 + 4 \cdot 5^2 + 3 \cdot 5^1 + 4 = 244.$$

One valid pair is

$$Y = (1, 4, 3, 2)_5 = 242, \quad Z = (3, 4, 2, 1)_5 = 486,$$

which share the digit multiset  $\{1, 2, 3, 4\}$  and satisfy  $X + Y = Z$ .