

# Trajan Algorithm

Input file:            **standard input**  
Output file:           **standard output**  
Time limit:            **2 seconds**  
Memory limit:         **1024 megabytes**

Recall the *Tarjan Algorithm* for calculating the articulation points (also called the cut vertices) in an undirected graph, whose pseudo-code is shown on the left.

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**Algorithm 1** The Correct Tarjan Algorithm

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```
1: function TARJAN( $i, d$ )
2:    $visited[i] \leftarrow \mathbf{true}$ 
3:    $depth[i] \leftarrow d$ 
4:    $low[i] \leftarrow d$ 
5:    $childCount \leftarrow 0$ 
6:    $isArticulation \leftarrow \mathbf{false}$ 
7:
8:   for each  $j$  in  $adj[i]$  do
9:     if  $j = parent[i]$  then
10:      continue
11:    end if
12:    if not  $visited[j]$  then
13:       $parent[j] \leftarrow i$ 
14:      TARJAN( $j, d + 1$ )
15:       $childCount \leftarrow childCount + 1$ 
16:      if  $low[j] \geq depth[i]$  then
17:         $isArticulation \leftarrow \mathbf{true}$ 
18:      end if
19:       $low[i] \leftarrow \min(low[i], low[j])$ 
20:    else
21:       $low[i] \leftarrow \min(low[i], depth[j])$ 
22:    end if
23:  end for
24:  if ( $parent[i] \neq \mathbf{null}$  and  $isArticulation$ )
   or ( $parent[i] = \mathbf{null}$  and  $childCount > 1$ )
   then
25:    Output  $i$  as articulation point
26:  end if
27: end function
```

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**Algorithm 2** The Incorrect Trajan Algorithm

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```
1: function TRAJAN( $i, d$ )
2:    $visited[i] \leftarrow \mathbf{true}$ 
3:    $depth[i] \leftarrow d$ 
4:    $low[i] \leftarrow d$ 
5:    $childCount \leftarrow 0$ 
6:    $isArticulation \leftarrow \mathbf{false}$ 
7:
8:   for each  $j$  in  $adj[i]$  do
9:     if  $j = parent[i]$  then
10:      continue
11:    end if
12:    if not  $visited[j]$  then
13:       $parent[j] \leftarrow i$ 
14:      TRAJAN( $j, d + 1$ )
15:       $childCount \leftarrow childCount + 1$ 
16:      if  $low[j] \geq depth[i]$  then
17:         $isArticulation \leftarrow \mathbf{true}$ 
18:      end if
19:    end if
20:     $low[i] \leftarrow \min(low[i], low[j])$ 
21:
22:
23:  end for
24:  if ( $parent[i] \neq \mathbf{null}$  and  $isArticulation$ )
   or ( $parent[i] = \mathbf{null}$  and  $childCount > 1$ )
   then
25:    Output  $i$  as articulation point
26:  end if
27: end function
```

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Note that in the pseudo code,  $adj[i]$  is the array containing all vertices adjacent to vertex  $i$ ,  $parent$  is an array in which the initial value of each element is null, and  $visited$  is an array in which the initial value of each element is false.

Some students may have a hard time understanding this algorithm, especially from line 19 to line 22. They can't understand why the *Tarjan Algorithm* needs to calculate the value of  $low[i]$  differently, and they may bear an incorrect version of the algorithm in mind. Let's call this incorrect version of the algorithm the *Trajan Algorithm*, which is shown on the right. Notice that the *Tarjan* and the *Trajan* algorithms are almost the same, except for the function names and the 4 lines from line 19 to line 22.

Given an undirected connected graph with  $n$  vertices and  $m$  edges, for each vertex  $u$  determine if there exists a vertex  $v$  and a 2-dimensional array  $adj$  ( $adj$  must represent the given graph) such that TARJAN( $v, 0$ ) and TRAJAN( $v, 0$ ) produce different results on vertex  $u$  (that is to say, the *Tarjan Algorithm* states that vertex  $u$  is an articulation point while the *Trajan Algorithm* does not, or vice versa).

## Input

There are multiple test cases. The first line of the input contains an integer  $T$  ( $1 \leq T \leq 10^4$ ) indicating the number of test cases. For each test case:

The first line contains two integers  $n$  and  $m$  ( $2 \leq n \leq 10^5$ ,  $1 \leq m \leq 10^5$ ) indicating the number of vertices and edges in the given graph.

For the following  $m$  lines, the  $i$ -th line contains two integers  $u_i$  and  $v_i$  ( $1 \leq u_i, v_i \leq n$ ) indicating that there is an edge connecting vertex  $u_i$  and  $v_i$  in the graph.

It's guaranteed that the given graph is connected and there are no self loops or multiple edges. Also, neither the sum of  $n$  nor the sum of  $m$  of all test cases will exceed  $10^6$ .

## Output

For each test case output one line containing some integers separated by one space in increasing order. Each integer is a vertex that the *Tarjan* and the *Trajan* algorithm may produce different results on. If there are no such vertices, output **Empty** in one line instead.

## Example

standard input	standard output
2	3 6 9
9 12	Empty
1 3	
2 3	
1 2	
3 6	
6 9	
9 3	
4 6	
5 6	
4 5	
7 9	
8 9	
7 8	
2 1	
1 2	

## Note

For the first sample test case:

- For  $u = 3$  consider  $v = 1$  and  $adj = [[3, 2], [3, 1], [1, 2, 6, 9], [6, 5], [6, 4], [4, 5, 3, 9], [9, 8], [9, 7], [7, 8, 3, 6]]$ .
- For  $u = 6$  consider  $v = 4$  and  $adj = [[2, 3], [1, 3], [9, 6, 2, 1], [6, 5], [6, 4], [4, 5, 3, 9], [9, 8], [9, 7], [7, 8, 3, 6]]$ .
- For  $u = 9$  consider  $v = 7$  and  $adj = [[2, 3], [1, 3], [9, 6, 2, 1], [5, 6], [4, 6], [9, 3, 5, 4], [9, 8], [9, 7], [7, 8, 3, 6]]$ .

Note that all *adjs* in the explanation are 1-indexed.